

4. (5 points) Evaluate the convolution of the two sequences $h(n)=(0.4)^n u(n)$ and $x(n)=2.1^n u(-n)$ by using the z -transform.

5. (6 points) Find the inverse of each of the following z -transforms:

(a) (1 point) $X(z) = 2 + 1.5(z^2 + z^{-2})$ $0 < |z| < \infty$

(b) (1 point) $X(z) = \frac{1}{1 - \frac{1}{2}z^{-1}} + \frac{3}{1 - \frac{1}{3}z^{-1}}$ $|z| > \frac{1}{2}$

(c) (2 point) $X(z) = \frac{2}{1 + 4z^{-1} + 3z^{-2}}$ $|z| > 3$

(d) (2 points) $X(z) = \frac{1 + \frac{1}{4}z^{-1}}{\left(1 + \frac{1}{2}z^{-1}\right)^2}$ $|z| > \frac{1}{2}$

6. (5 points) A signal $y(n)$ contains a primary signal, $x(n)$, plus two echoes:

$$y(n) = x(n) + \frac{1}{3}x(n - n_d) + \frac{1}{6}x(n - 2n_d)$$

Find a *realizable* filter that will recover $x(n)$ from $y(n)$.